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CITATION:

Gongyo, Shinya ...[et al]. Off-diagonal gluon mass generation and infrared Abelian dominance in maximally Abelian gauge in SU(3) lattice QCD. Physical Review D 2012, 86(9): 094018.

ISSUE DATE:

2012-11-13

URL:

<http://hdl.handle.net/2433/198849>

RIGHT:

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Off-diagonal gluon mass generation and infrared Abelian dominance in maximally Abelian gauge in SU(3) lattice QCD

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(Received 28 August 2012; published 13 November 2012)

In SU(3) lattice QCD formalism, we propose a method to extract gauge fields from link variables analytically. With this method, we perform the first study on effective mass generation of off-diagonal gluons and infrared Abelian dominance in the maximally Abelian gauge in the SU(3) case. Using SU(3) lattice QCD, we investigate the propagator and the effective mass of the gluon fields in the maximally Abelian gauge with $U(1)_3 \times U(1)_8$ Landau gauge fixing. The Monte Carlo simulation is performed on 16^4 at $\beta = 5.7, 5.8$, and 6.0 at the quenched level. The off-diagonal gluons behave as massive vector bosons with the approximate effective mass $M_{\text{off}} \simeq 1.0\text{--}1.1$ GeV in the region of $r = 0.3\text{--}0.8$ fm, and the propagation is limited within a short range, while the propagation of diagonal gluons remains even in a large range. In this way, infrared Abelian dominance is shown in terms of short-range propagation of off-diagonal gluons. Furthermore, we investigate the functional form of the off-diagonal gluon propagator. The functional form is well described by the four-dimensional Euclidean Yukawa-type function $e^{-m_{\text{off}}r}/r$ with $m_{\text{off}} \simeq 1.2\text{--}1.3$ GeV for $r = 0.1\text{--}0.8$ fm. This also indicates that the spectral function of off-diagonal gluons has the negative-value region.

DOI: [10.1103/PhysRevD.86.094018](https://doi.org/10.1103/PhysRevD.86.094018)

PACS numbers: 12.38.Aw, 12.38.Gc, 14.70.Dj

I. INTRODUCTION

Quantum chromodynamics (QCD) is the fundamental gauge theory of the strong interaction based on quarks and gluons. There are a variety of nonperturbative phenomena in low-energy QCD such as color confinement and chiral symmetry breaking. These nonperturbative phenomena have been studied both in analytical frameworks and in lattice QCD [1–3].

On the quark-confinement mechanism, Nambu, 't Hooft, and Mandelstam suggested the dual-superconductor picture [4]. This picture is based on the electromagnetic duality and the analogy with the one-dimensional squeezing of the magnetic flux in the type-II superconductor. In this picture, there occurs color magnetic monopole condensation, and then the color-electric flux between the quark and the antiquark is squeezed as a one-dimensional tube due to the dual Higgs mechanism. From the viewpoint of the dual-superconductor picture in QCD, however, there are two assumptions of Abelian dominance [5,6] and monopole condensation. Here, Abelian dominance means that only the diagonal gluon component plays the dominant role for the nonperturbative QCD phenomena like confinement.

The maximally Abelian (MA) gauge has mainly been investigated from the viewpoint of the dual-superconductor picture [7–19] and the various lattice QCD Monte Carlo

simulations show that the MA gauge fixing seems to support these assumptions [10–19].

According to these studies, the diagonal gluons seem to be significant to the infrared QCD physics, which is called “infrared Abelian dominance.” Infrared Abelian dominance means that off-diagonal gluons do not contribute to infrared QCD. Therefore, the essence of infrared Abelian dominance is the behavior of the off-diagonal gluon propagator.

The gluon propagators in the MA gauge has been investigated in SU(2) lattice Monte Carlo simulations [18–20]. To investigate the gluon propagators in the MA gauge, it is desired to extract the gluons exactly from the link variables, because the link variable cannot be expanded even for a small lattice spacing due to the large fluctuation of gluons. In SU(2) lattice case, the extraction is easy to be done without any approximation, because of the SU(2) property. With this extraction, the SU(2) lattice simulation suggests that the off-diagonal gluons do not propagate in the infrared region due to the effective mass $M_{\text{off}} \simeq 1.2$ GeV, while the diagonal gluon widely propagates [18].

The aim of this paper is to propose a method to extract the gluons from the link variable directly and generally in SU(3) lattice QCD, and to investigate the gluon propagators in the MA gauge.

II. SU(3) FORMALISM AND GLUON PROPAGATORS IN MA GAUGE WITH $U(1)_3 \times U(1)_8$ LANDAU GAUGE

Using the SU(3) lattice QCD, we calculate the gluon propagators in the MA gauge with the $U(1)_3 \times U(1)_8$

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Landau gauge fixing. In the MA gauge, to investigate the gluon propagators, we use the gluon fields extracted directly from the link variables [21]. Here, we analytically extract the gluon field $A_\mu(x)$ from each link variable $U_\mu(x)$ as follows:

$$A_\mu(x) = \frac{1}{iag} \text{Ln} U_\mu(x) = \frac{1}{iag} \Omega_\mu^\dagger(x) \text{Ln} U_\mu^d(x) \Omega_\mu(x), \quad (1)$$

where Ln is the natural logarithm defined on complex numbers, $U_\mu^d(x)$ is the diagonalized unitary matrix, and $\Omega_\mu(x)$ is the diagonalization unitary matrix of eigenvectors.

The MA gauge fixing is performed by the maximization of

$$R_{\text{MA}} \equiv \sum_x \sum_{\mu=1}^4 \text{tr}[U_\mu(x) \vec{H} U_\mu^\dagger(x) \vec{H}], \quad (2)$$

where $\vec{H} = (T_3, T_8)$ is the Cartan generator. In this gauge fixing, there remains $U(1)_3 \times U(1)_8$ gauge symmetry. In order to study the gluon propagators, we fix the residual gauge. After the Cartan decomposition for the $SU(3)$ link variables as $U_\mu(x) \equiv M_\mu(x) u_\mu(x)$ with $u_\mu(x) \equiv e^{i(\theta^3(x)T^3 + \theta^8(x)T^8)} \in U(1)_3 \times U(1)_8$ and $M_\mu(x) = e^{i\sum_{a \neq 3,8} \theta^a(x)T^a} \in SU(3)/U(1)_3 \times U(1)_8$, the residual gauge fixing is performed by the maximization of

$$R_{U(1)_L} \equiv \sum_x \sum_{\mu=1}^4 \text{Re tr}[u_\mu(x)]. \quad (3)$$

At $\beta = 5.7, 5.8$, and 6.0 , the lattice spacings a are estimated as $a \simeq 0.186$ fm, 0.152 fm, and 0.104 fm, respectively, which lead to the string tension $\sigma \simeq 0.89$ GeV/fm in the interquark potential [22].

After gauge fixing completely, we study the Euclidean scalar combination of the diagonal (Abelian) gluon propagator as

$$G_{\mu\mu}^{\text{Abel}}(r) \equiv \frac{1}{2} \sum_{a=3,8} \langle A_\mu^a(x) A_\mu^a(y) \rangle, \quad (4)$$

and that of the off-diagonal gluon propagator as

$$G_{\mu\mu}^{\text{off}}(r) \equiv \frac{1}{6} \sum_{a \neq 3,8} \langle A_\mu^a(x) A_\mu^a(y) \rangle. \quad (5)$$

These are expressed as the function of the four-dimensional Euclidean distance $r \equiv \sqrt{(x_\mu - y_\mu)^2}$. When we consider the renormalization, these propagators are multiplied by an r -independent constant, according to the renormalized gluon fields obtained by multiplying a constant renormalization factor.

The Monte Carlo simulation is performed with the standard plaquette action on the 16^4 lattice with $\beta = 5.7, 5.8$,

and 6.0 at the quenched level. All measurements are done every 500 sweeps after a thermalization of 10,000 sweeps using the pseudo-heatbath algorithm. We prepare 50 gauge configurations for the calculation at each β . The error is estimated with the jackknife analysis.

We show in Fig. 1 the lattice QCD result for the diagonal gluon propagator $G_{\mu\mu}^{\text{Abel}}(r)$ and the off-diagonal gluon propagator $G_{\mu\mu}^{\text{off}}(r)$ in the MA gauge with the $U(1)_3 \times U(1)_8$ Landau gauge fixing. In the MA gauge, $G_{\mu\mu}^{\text{Abel}}(r)$ and $G_{\mu\mu}^{\text{off}}(r)$ manifestly differ. The diagonal-gluon propagator $G_{\mu\mu}^{\text{Abel}}(r)$ takes a large value even at the long distance. In fact, the diagonal gluons A_μ^3, A_μ^8 in the MA gauge propagate over the long distance. On the other hand, the off-diagonal gluon propagator $G_{\mu\mu}^{\text{off}}(r)$ rapidly decreases and is negligible for $r \geq 0.4$ fm in comparison with $G_{\mu\mu}^{\text{Abel}}(r)$. Then, the off-diagonal gluons $A_\mu^a (a \neq 3, 8)$ seem to propagate only within the short range as $r \leq 0.4$ fm. Thus, infrared Abelian dominance is found in the MA gauge.

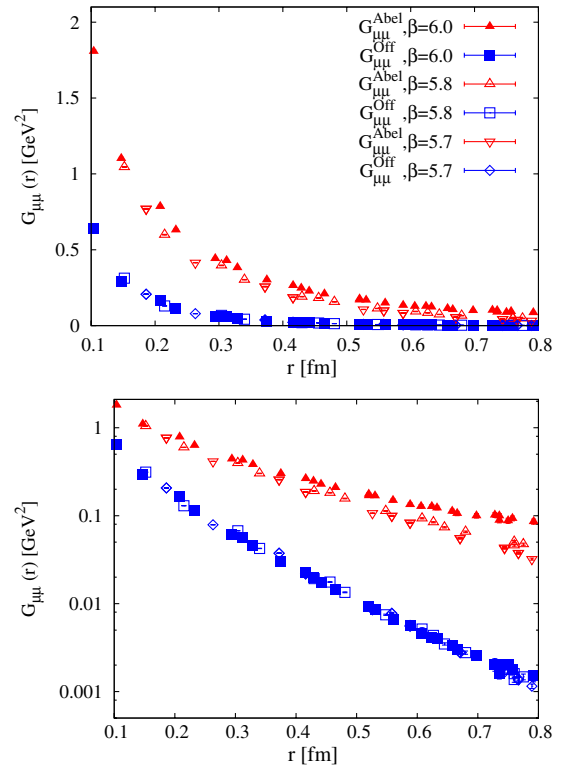


FIG. 1 (color online). The $SU(3)$ lattice QCD results of $G_{\mu\mu}^{\text{Abel}}(r)$ and $G_{\mu\mu}^{\text{off}}(r)$ (top panel), and their logarithmic plots (bottom panel) as the function of $r \equiv \sqrt{(x_\mu - y_\mu)^2}$ in the MA gauge with the $U(1)_3 \times U(1)_8$ Landau gauge fixing in the physical unit. The Monte Carlo simulation is performed on the 16^4 lattice with $\beta = 5.7, 5.8$ and 6.0 . The diagonal-gluon propagator $G_{\mu\mu}^{\text{Abel}}(r)$ takes a large value even at the long distance. On the other hand, the off-diagonal gluon propagator $G_{\mu\mu}^{\text{off}}(r)$ rapidly decreases.

III. ESTIMATION OF OFF-DIAGONAL GLUON MASS IN MA GAUGE

Next, we investigate the effective gluon mass. We start from the Lagrangian of the free massive vector field A_μ with the mass $M \neq 0$ in the Proca formalism,

$$\mathcal{L} = \frac{1}{4}(\partial_\mu A_\nu - \partial_\nu A_\mu)^2 + \frac{1}{2}M^2 A_\mu A_\mu, \quad (6)$$

in the Euclidean metric. The scalar combination of the propagator $G_{\mu\mu}(r; M)$ can be expressed with the modified Bessel function $K_1(z)$ as

$$\begin{aligned} G_{\mu\mu}(r; M) &= \langle A_\mu(x) A_\mu(y) \rangle \\ &= \int \frac{d^4 k}{(2\pi)^4} e^{ik \cdot (x-y)} \frac{1}{k^2 + M^2} \left(4 + \frac{k^2}{M^2} \right) \\ &= 3 \int \frac{d^4 k}{(2\pi)^4} e^{ik \cdot (x-y)} \frac{1}{k^2 + M^2} + \frac{1}{M^2} \delta^4(x-y) \\ &= \frac{3}{4\pi^2} \frac{M}{r} K_1(Mr) + \frac{1}{M^2} \delta^4(x-y). \end{aligned} \quad (7)$$

In the infrared region with large Mr , Eq. (7) reduces to

$$G_{\mu\mu}(r; M) \simeq \frac{3\sqrt{M}}{2(2\pi)^{\frac{3}{2}}} \frac{e^{-Mr}}{r^{\frac{3}{2}}}, \quad (8)$$

using the asymptotic expansion,

$$K_1(z) \simeq \sqrt{\frac{\pi}{2z}} e^{-z} \sum_{n=0}^{\infty} \frac{\Gamma(\frac{3}{2} + n)}{n! \Gamma(\frac{3}{2} - n)} \frac{1}{(2z)^n}, \quad (9)$$

for large $\text{Re} z$.

In Fig. 2, we show the logarithmic plot of $r^{3/2} G_{\mu\mu}^{\text{off}}(r)$ and $r^{3/2} G_{\mu\mu}^{\text{Abel}}(r)$ as the function of the four-dimensional

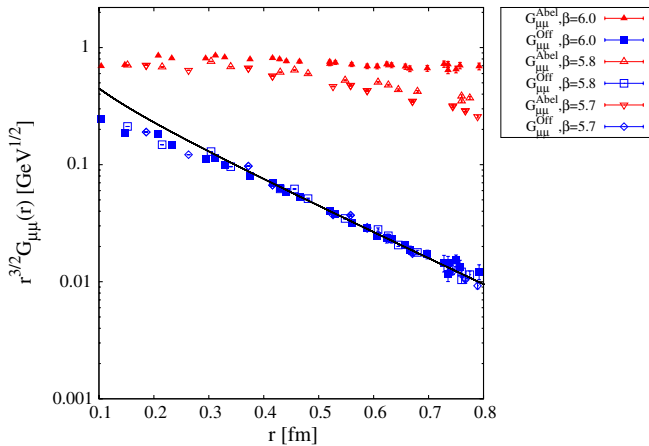


FIG. 2 (color online). The logarithmic plot of $r^{3/2} G_{\mu\mu}^{\text{off}}(r)$ and $r^{3/2} G_{\mu\mu}^{\text{Abel}}(r)$ as the function of the four-dimensional Euclidean distance r in the MA gauge with the $U(1)_3 \times U(1)_8$ Landau gauge fixing, using the SU(3) lattice QCD with 16^4 at $\beta = 5.7, 5.8$ and 6.0 . The solid line denotes the logarithmic plot of $r^{3/2} G_{\mu\mu}(r) \sim r^{1/2} K_1(Mr)$ in the Proca formalism.

TABLE I. Summary table of conditions and results in SU(3) lattice QCD. The off-diagonal gluon mass M_{off} is estimated from the slope analysis of $r^{3/2} G_{\mu\mu}^{\text{off}}(r)$ for $r = 0.3\text{--}0.8$ fm at each β . In the MA gauge, the off-diagonal gluons seem to have a large effective mass of $M_{\text{off}} \simeq 1.0\text{--}1.1$ GeV. The best-fit mass parameter m_{off} is also listed at each β : $G_{\mu\mu}^{\text{off}}(r)$ in the range of $r = 0.1\text{--}0.8$ fm is well described with the four-dimensional Euclidean Yukawa function $\sim e^{-m_{\text{off}} r}/r$ with $m_{\text{off}} \simeq 1.2\text{--}1.3$ GeV. We add the diagonal gluon effective mass M_{diag} at each β , estimated in a similar manner to M_{off} .

Lattice size	β	a [fm]	M_{off} [GeV]	m_{off} [GeV]	M_{diag} [GeV]
16^4	5.7	0.186	1.1	1.2	0.1
	5.8	0.152	1.0	1.2	0.3
	6.0	0.104	1.0	1.3	0.4

Euclidean distance r in the MA gauge with the $U(1)_3 \times U(1)_8$ Landau gauge fixing. From the linear slope on $r^{3/2} G_{\mu\mu}^{\text{off}}(r)$, the effective off-diagonal gluon mass M_{off} is estimated. Note that the gluon-field renormalization does not affect the gluon mass estimate, since it gives only an overall constant factor for the propagator. We summarize in Table I the effective off-diagonal gluon mass M_{eff} obtained from the slope analysis in the range of $r = 0.3\text{--}0.8$ fm at $\beta = 5.7, 5.8$ and 6.0 . The off-diagonal gluons seem to have a large effective mass of $M_{\text{off}} \simeq 1.0\text{--}1.1$ GeV. This result approximately coincides with SU(2) lattice calculation [18].

Also for the diagonal gluon, we try to estimate its effective mass M_{diag} , although its propagator largely depends on β , i.e., the volume or the spacing, as is indicated in Fig. 2. We estimate the diagonal gluon mass M_{diag} from the slope analysis in the range of $r = 0.3\text{--}0.8$ fm at each β , and add the result in Table I. In any case, the diagonal gluon seems to have a small effective mass of $M_{\text{diag}} \simeq 0.1\text{--}0.4$ GeV. For the definite argument on $G_{\mu\mu}^{\text{Abel}}(r)$ and the diagonal gluon mass, more careful analysis with a large-volume lattice would be needed.

Finally in this section, we discuss the relation between infrared Abelian dominance and the off-diagonal gluon mass. Due to the large effective mass M_{off} , the off-diagonal gluon propagation is restricted within about $M_{\text{off}}^{-1} \simeq 0.2$ fm in the MA gauge. Therefore, at the infrared scale as $r \gg 0.2$ fm, the off-diagonal gluons $A_\mu^a (a \neq 3, 8)$ cannot mediate the long-range force like the massive weak bosons in the Weinberg-Salam model, and only the diagonal gluons A_μ^3, A_μ^8 can mediate the long-range interaction in the MA gauge. In fact, in the MA gauge, the off-diagonal gluons are expected to be inactive due to the large mass M_{off} in the infrared region in comparison with the diagonal gluons. Then, infrared Abelian dominance holds for $r \gg M_{\text{off}}^{-1}$.

IV. ANALYSIS OF FUNCTIONAL FORM OF OFF-DIAGONAL GLUON PROPAGATOR IN MA GAUGE

In this section, we investigate the functional form of the off-diagonal gluon propagator in the MA gauge in SU(3)

lattice QCD. In the previous section, we compare the gluon propagator with the massive vector boson propagator and estimate the gluon mass. In fact, as shown in Fig. 2, the gluon propagator would not be described by a simple massive propagator Eq. (7) in whole region of $r = 0.1\text{--}0.8$ fm.

There is the similar situation in the Landau gauge [22]. The functional form of the gluon propagator cannot be described by the propagator of the Proca formalism in whole region of $r = 0.1\text{--}1.0$ fm. The appropriate form is the four-dimensional Euclidean Yukawa-type function $\exp(-mr)/r$ with a mass parameter m .

In the same way, in the MA gauge, we also compare the gluon propagator with the four-dimensional Euclidean Yukawa function. In Fig. 3, we show the logarithmic plot of $rG_{\mu\mu}^{\text{off}}(r)$ and $rG_{\mu\mu}^{\text{Abel}}(r)$ as the function of the distance r in the MA gauge with the $U(1)_3 \times U(1)_8$ Landau gauge fixing. Note that, in the whole region of $r = 0.1\text{--}0.8$ fm, the logarithmic plot of $rG_{\mu\mu}^{\text{off}}(r)$ is almost linear, and therefore the off-diagonal gluon propagator is well expressed by the four-dimensional Euclidean Yukawa function,

$$G_{\mu\mu}^{\text{off}}(r) \simeq A \frac{e^{-m_{\text{off}} r}}{r}, \quad (10)$$

with a mass parameter m_{off} and a dimensionless constant A . The best-fit mass parameter m_{off} is given in Table I at each $\beta = 5.7, 5.8$, and 6.0 .

We comment on the four-dimensional Euclidean Yukawa-type propagator [22]. If the functional form of the off-diagonal gluon is well described by the four-dimensional Yukawa function, we analytically calculate the off-diagonal zero-spatial-momentum propagator,

$$D_0^{\text{off}}(t) \equiv \int d^3x G_{\mu\mu}^{\text{off}}(r), \quad (11)$$

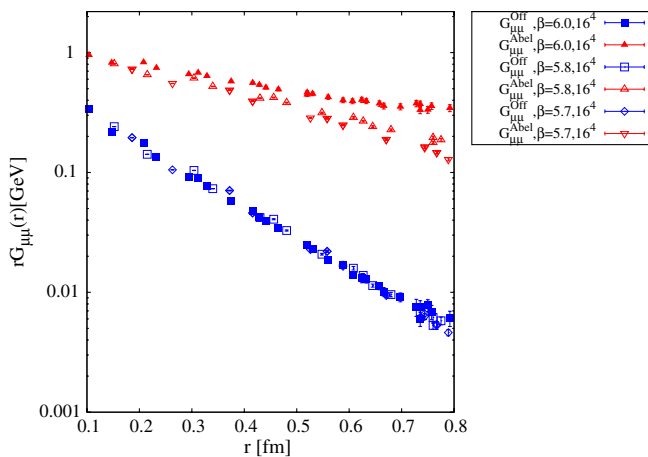


FIG. 3 (color online). The logarithmic plot of $rG_{\mu\mu}^{\text{off}}(r)$ and $rG_{\mu\mu}^{\text{Abel}}(r)$ as the function of the four-dimensional Euclidean distance r in the MA gauge with the $U(1)_3 \times U(1)_8$ Landau gauge fixing, using the SU(3) lattice QCD with 16^4 at $\beta = 5.7, 5.8$ and 6.0 . For $rG_{\mu\mu}^{\text{off}}(r)$, the approximate linear correlation is found.

and obtain the spectral function $\rho(\omega)$ by the inverse Laplace transformation. Also in the MA gauge, the spectral function is found to have the negative-value region, as in the Landau gauge [22–24].

V. SUMMARY AND CONCLUDING REMARKS

We have performed the first study on the gluon propagators in the MA gauge with the $U(1)_3 \times U(1)_8$ Landau gauge fixing using the SU(3) lattice QCD. To investigate the gluon propagators in the MA gauge, we have considered to derive the gluon fields from the SU(3) link variables. In this method, the gauge fields have been extracted by diagonalizing the link variables and taking the logarithm. Owing to this method, any quantity expressed by the gluon fields can be calculated directly from link variables, even if $|agA_\mu(x)| \ll 1$ does not satisfy. As one of the general merits of this method, we can directly check the correspondence between gluon fields and the continuum gauge fixing in arbitrary lattice gauge fixing performed with link variables. In principle, with this method, continuum gauge fixing with gluon fields can be also performed directly.

With this method, we have measured the Euclidean scalar combinations of the propagators $G_{\mu\mu}(r)$ for the diagonal and the off-diagonal gluons, and found the infrared Abelian dominance. The Monte Carlo simulation is performed on the 16^4 lattice with $\beta = 5.7, 5.8$, and 6.0 at the quenched level. We have found that the off-diagonal gluons behave as massive vector bosons with the effective mass $M_{\text{off}} \simeq 1.0\text{--}1.1$ GeV for $r = 0.3\text{--}0.8$ fm. The effective gluon mass has been estimated from the linear fitting analysis of the logarithmic plot of $r^{3/2}G_{\mu\mu}^{\text{off}}(r)$. Due to the large value, the finite-size effect for the off-diagonal gluon mass is expected to be ignored. The large gluon mass shows that the off-diagonal gluons cannot mediate the interaction over the large distance as $r \gg M_{\text{off}}^{-1}$, and such an infrared inactivity of the off-diagonal gluons would lead infrared Abelian dominance in the MA gauge.

On the other hand, from the behavior of the diagonal gluon propagator $G_{\mu\mu}^{\text{Abel}}(r)$ and $r^{3/2}G_{\mu\mu}^{\text{Abel}}(r)$, the diagonal gluons seem to behave as light vector bosons with the effective mass $M_{\text{diag}} \simeq 0.1\text{--}0.4$ GeV for $r = 0.3\text{--}0.8$ fm, although careful analysis with a large-volume lattice is needed for more definite argument on $G_{\mu\mu}^{\text{Abel}}(r)$.

Finally, we have also investigated the functional form of the propagator in the MA gauge. We show that the off-diagonal gluon propagator $G_{\mu\mu}^{\text{off}}(r)$ is well described by the four-dimensional Euclidean Yukawa-type form with the mass parameter $m_{\text{off}} \simeq 1.2\text{--}1.3$ GeV in the region of $r = 0.1\text{--}0.8$ fm. This indicates that the spectral function $\rho(\omega)$ of the off-diagonal gluons in the MA gauge has the negative-value region as in the Landau gauge.

On the other hand, the functional form of the diagonal gluon propagator seems to be the four-dimensional Euclidean Yukawa function with the lighter mass parameter. However, to discuss the functional form clearly, the finite size effect is to be checked carefully just like the estimation of the diagonal effective gluon mass.

In this study, we investigate the off-diagonal gluon propagator. To be strict, the off-diagonal gluon propagator consists of two scalar functions corresponding to longitudinal and transverse components. Therefore, we will investigate each effective mass and the functional form of these components.

ACKNOWLEDGMENTS

The authors are deeply grateful to Dr. Hideaki Iida for useful discussions. This work is supported in part by the Grant for Scientific Research [(C) No. 23540306, Priority Areas “New Hadrons” (E01:21105006)]; Grant-in-Aid for JSPS Fellows (Grant No. 23-752, 24-1458) from the Ministry of Education, Culture, Science and Technology (MEXT) of Japan; and the Global COE Program, “The Next Generation of Physics, Spun from Universality and Emergence.” The lattice QCD calculations were done on NEC SX-8R at Osaka University.

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